# ON THE DEPRESSION OF $T_c$ OF REBa $_2$ Cu $_3$ O $_{7-\delta}$ (RE = Y, Er) DUE TO NI $^{2+}$ SUBSTITUTION INTO THE Cu(2) SITES. (s + d)-WAVE MODEL INTERPRETATION

K. KONGSAKULYANON, W. TANGTATHARAKUL AND I.M. TANG

- <sup>a</sup> Department of Physics, Faculty of Science & Technology, Rangsit Campus Thammasat University, Patum Thani 12121, Thailand.
- b Department of Physics, Faculty of Science Mahidol University, Bangkok 10400, Thailand.

(Received May 3, 1998)

## **ABSTRACT**

The depressions of the  $T_c$ 's of two  $\varsigma$ 123é ReBa $_2$ Cu $_3$ O $_7$  (Re = Y, Er) HTSC's due to magnetic (Ni $^2$ +) transition metal substitution into the Cu(2) layer are studied. Special attention is paid to the difference in the orthorhombicity ( $\mathbf{D} = (\mathbf{b} \cdot \mathbf{a})/\mathbf{a}$ , where  $\mathbf{a}$  and  $\mathbf{b}$  are the lattice parameters in the basal plane) of the two superconductors. It is observed that the rate of depression  $dT_c/dx$  for the  $\varsigma$ Y-123é HTSC is slightly steeper than that for the  $\varsigma$ Er-123é HTSC. The difference in the rates of depression is explained in terms of a connection between the orthorhombicity and the superconducting state. It is assumed that the orthorhombic distortion induces a change in the pairing interaction. The modification of the pairing interaction leads to a new superconducting state in which order parameter ( $\mathbf{OP}$ ) has ( $\mathbf{s} + \mathbf{d}$ )-wave symmetry.

### I. INTRODUCTION.

Shortly after the discovery of 90 K superconductivity in the YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7-v</sub> high temperature superconductor (HTSC),1 different groups2 studied the replacement of the Y ions by rare earth (RE) ions. When it was reported that the Tc's did not change in any systematic way, the conclusion was drawn that superconductivity in the HTSC's was two dimensional in nature and that the pair condensation occurred in the planar CuO2 layer. Since several of the RE ions are magnetic, the absence of any apparent differences between these "RE-123" HTSC's and the YBa2Cu3O2-v HTSC was taken as evidence there was not much interaction between the Y or RE ions and the carriers in the CuO2 layer. Other groups³ chose to study the replacement of the Cu ions in this ("123") and other HTSC's by other transition metal ions, both magnetic (  $Ni^{2+}$ ,  $Fe^{3+}$  and  $Co^{3+}$ ) and non magnetic (  $Zn^{2+}$  and  $Al^{2+}$  ) ions. The investigators of refs. 3 found that both the magnetic and non magnetic TM ions substitutions suppress the superconductivity. The suppression of the  $T_c$ 's by non magnetic  $Zn^{2+}$  was surprising since in conventional superconductors, non magnetic ion doping has negligible effects on the superconducting state.<sup>4</sup> The suppression of  $T_c$  in the "123" HTSC by  $Zn^{2+}$  ion substitution is even greater than that due to Ni<sup>2+</sup> ion substitution.<sup>5</sup> This was the first indication that the elph interaction was not responsible for the pair condensation in the HTSC's.

Another discovery which clearly indicated that pair condensation in the HTSC's was not due to the el-ph interaction was the observation that the order parameters (OP) of the HTSC's exhibited d-wave symmetry. <sup>6,7</sup> This requires a new mechanism be responsible for superconductivity in the HTSC's since the el-ph interaction leads to an OP of s-wave symmetry. This lead Monthoux and Pines<sup>8</sup> (MP) to propose that the pair condensation in the HTSC was

due to the exchange of the antiferromagnetic spin fluctuations (SF) which occurs in the  $2D CuO_2$  plane. The exchange of these SF leads uniquely to a superconducting state of d-wave symmetry. The theory also accounted for the difference in the relative magnitude of the depressions of the  $T_c$ 's due to  $Ni^{2+}$  and to  $Zn^{2+}$  substitutions. In this theory, the Zn ions disrupts the propagation of the SF in the 2D plane and thus affects the mechanisms responsible for the pair condensation while the magnetic Ni ions breaks the pairs **after** they are formed. In the first instance, the influence on the superconducting state is a direct one while in the second instance, the influence is an indirect one.

The recent discoveries<sup>9</sup> that the OP of YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7-y</sub> HTSC contains a s-wave component requires a change in the SF-induced pairing mechanism in the MP theory. A basic principle in physics is that any potential or interaction existing in a space must be invariant under the group operations which leave the space invariant. One of the reasons for MP to propose the exchange of SF as being the mechanism responsible for superconductivity in the HTSC's is that the SF-induced pairing interaction would have the symmetry of the CuO<sub>2</sub> layer, i.e., tetragonal symmetry. The orthorhombic distortion of the crystal structure occurring in the "123" perovskite ceramics would be expect to induce a change in the symmetry of the pairing interaction so that it remains invariant under the new symmetry operations for the new structure.

One of the present authors (IMT) has used this idea to find the dependence of the  $T_c$ 's of the "RE-123" HTSC's on the orthorhombicity of the RE ions. One As mentioned earlier, the first sets of measurements of the  $T_c$ 's of the "RE-123" HTSC did not reveal any dependence on the size of the RE ions. These measurements were done on specimens for which the hole concentrations was not monitored. Later sets of measurements on specimens for which the oxygen content or hole concentration were kept constant revealed a dependence of the  $T_c$ 's on the size of the RE ions. The rare earth ion size and the orthorhombicity are related to each other. The orthorhombic distortion in the "123" occur when  $O^2$  ions are removed from sites in the  $\bf a$  direction of the third  $CuO_2$  layer in the triple perovskite  $YBa_2Cu_3O_8$ . The removal of these ions leaves behind 1D CuO chains in the  $\bf b$  direction. The chains then collapse towards each other, thus causing the  $\bf a$  lattice parameter to be smaller than the  $\bf b$  lattice parameter. Substitution of larger Re ions arrest the collapse of the chains towards each other and thus effect the degree of orthorhombicity.

Tang et al., 12 recently extended the ideas used ref. 10 to find a rare earth ion size dependence of the rates of depression of  $T_c$  due to TM ion substitution. That work was motivated in part by a study of Sumana Prabhu and Varadaraju 13 on the suppression of superconductivity in REBa<sub>2</sub>Cu<sub>3-x</sub>M<sub>x</sub>O<sub>7</sub> (RE = Sm and Dy) by Fe, Ni and Zn substitution. We wish to report our study of the depression of  $T_c$ 's of YBa<sub>2</sub>Cu<sub>3-x</sub>M<sub>x</sub>O<sub>7</sub> and ErBa<sub>2</sub>Cu<sub>3-x</sub>M<sub>x</sub>O<sub>7</sub> due to Ni<sup>2+</sup> substitution. Only Ni<sup>2+</sup> substitution is considered here since Co<sup>3+</sup> and Fe<sup>3+</sup> ions enter preferentially into the Cu(1) sites in the 1D CuO chain and the special scattering process proposed for Zn<sup>2+</sup> in the Monthoux and Pines theory is still controversial. We will explain our findings in terms of the modification of the pairing interaction induced by the orhorhombic distortion occurring in the "123" ceramics as oxygen is removed from O sites located in the direction of the **a** lattice.

# II. EXPERIMENTAL DETAILS AND RESULTS.

The high temperature superconductors were prepared by the standard ceramic method. Stoichiometric amounts of  $ER_2O_3$ ,  $Y_2O_3$ ,  $BaCO_3$ , CuO and NiO were carefully weight and mixed in a aggate motar to obtain the two series,  $YBa_2Cu_{3-x}Ni_xO_7$  and  $ErBa_2Cu_{3-x}Ni_xO_7$  (x = 1).

0.0, 0.004, 0.008, 0.010 and 0.015 ). The mixtures were calcinated at 920 C for 24 hrs. They were then reground and pressed into pellets of approximately one cm in diameter and 2 mm in thickness. These were then sintered in a furnace at 920 C for another 24 hrs., after which they were cooled to room temperature in a flowing  $O_2$  atmosphere at the rate of 1°C/min. The proper hole concentrations were achieved during the slow cooling down cycle. XRD patterns were obtained on each specimens. The temperatures were monitored with a carbon glass thermometer. The resistivities were measured using the standard four probe method.  $T_c$  is defined as the temperature at which the resistance extrapolates to zero.

The results of the determination of the lattice parameters  $\bf a$  and  $\bf b$  for the specimens are listed in Table 1. As we see, there are small changes in these parameters (at the third decimal place) as the Ni²+ ions are initially added. The orthorhombicity were calculated and range from 1.522 to 1.841 ( x 10²) for the ( pure and doped ) YBa₂Cu₃O₂ and from 1.532 to 1.862 for the ( pure and doped ) ErBa₂Cu₃O₂. The averaged orthorhombicities were 1.756 and 1.731, respectively and differ by only 1.4%. Sumana Prabhu and Varadaraju¹³ report that the  $\bf a$  and  $\bf b$  lattice parameters in the çSm-123é ceramics changed rapidly as Ni²+ was added. The orthorhombicity D decreased monotonically, going to zero at  $\bf x=0.6$ . The çDy-123é ceramic remained orthorhombic throughout the entire Ni doping range. For Ni concentrations below 0.04, the orthorhombicities of the "Dy-123" ceramics varied only slightly. Since the impurity concentrations used in our study are very low, we did not expect to see any evidence of any O-T transition, even if one were to occur.

The measured  $T_c$ 's of the "Y-123" and "Er-123" HTSC are 94.4 K and 91.3 K, respectively. The relative order of the  $T_c$ 's of the "Er-123" and "Y-123" HTSC's, i.e.,  $T_{c.Er-123} < T_{c.Y-123}$ , is consistent with the observations made in refs. 11. Interestingly, the T's of the host "Re-123" HTSC's reported by Sumana Prabhu and Varadaraju<sup>13</sup> (SV) did not exhibit any dependence on the rare earth ions, i.e., they were all the same ( about 90 K ). We have pointed out this may be due to variability of the hole concentration in the superconductors. On Figs. 1a and 1b, we show the depression of the T's of these two HTSC's as Ni2+ ions are substituted into the Cu(2) sites. As is seen, the decreases of the T<sub>c</sub>'s of both the "Y-123" series and the "Er-123" series are characterized by a rapid initial decrease, followed by an almost linear decrease as x ( Ni content ) is increased from 0.002 to 0.008. In these portions of the curves, the rates of decrease due to  $Ni^{2+}$  substitution, dT/dx, is 2.29 K/at.% for the "Y-123" series and is 2.16 K/ at.% for the "Er-123" series. Our results on the relative magnitudes of the rates of decrease, i.e.,  $dT/dx_v < dT/dx_{Fr}$  due to Ni substitutions, are consistent with the results of ref. 13. SV looked at the effects of TM impurity substitution into the REBa<sub>2</sub>Cu<sub>3-x</sub> $M_xO_7$  ( RE = Sm and Dy; M = Fe, Ni and Zn ) HTSC's. They found that the rates of decrease of the  $T_c$ 's due to the three TM impurities for the "Sm-123" HTSC were greater than the rates of decrease for the "Dy-123" HTSC. These decreases inturn are less than those of the "Nd-123" HTSC but higher than those for the Y-123. SV quote a value of 3 K/at.% for the rate of depression of T, due to Ni substitution into the "Y-123" HTSC. ( Note: our value is 2.29 K/at.% ). The decrease in the ionic radii of Nd, Sm, Dy and Y goes as 1.109 A, 1.079 A, 1.027 A and 1.019 A. The radius of the Er ion is smaller than that of Y and so the relative magnitude of the rate of decrease due to Ni<sup>2+</sup> fits into the trend seen by SV. Sumana Prabhu and Varadaraju could only conjecture on the reasons for the Re ion size effect of the rates of decreases in the Tc's due to the 3d substitution.

### III. THEORETICAL ASPECTS.

As we have pointed out, the orthorhombic distortion which occurs in the "Re-123" HTSC's induces a modification of the tetragonal spin-fluctuation pairing interaction. Such a modification could be $^{10}$ 

$$V_{\text{pair}}(\mathbf{q}, \mathbf{q}'; \omega) = V_{\text{SF}} + \alpha(D) \{ V_{\text{ani}}[ \eta(\mathbf{q}) + \eta(\mathbf{q}') ] + V_{\text{iso}} \} - \mu$$
 (1)

where  $V_{SF}$  is the spin fluctuation-induced pairing interaction in the MP theory;  $V_{ani}$ , an non separable anisotropic interaction induced by the orhorhombic distortion;  $V_{iso}$ , the isotropic pairing interaction also induced by the distortion and which gives rise to the s-wave component of the OP;  $\alpha(D)$ , a parameter which depends on the orthorhombicity D and which is zero in the absence of the orthorhombic distortion.  $\eta($ ) is a basis function for a representation of the crystal symmetry group.  $\mu$  is the Coulomb repulsion term and will be neglected in all further calculations.

The order parameter (OP) as in any theory of superconductivity is defined as

$$\Delta(\mathbf{k}, \omega_{n}) = 2\pi T \sum \int \frac{dS \mathbf{p}}{8\pi^{3} V_{F}} V_{pair}(\mathbf{k} - \mathbf{p}; \omega_{n} - \omega_{m}) \frac{\Omega(\mathbf{p}, \omega_{m})}{\sqrt{(|\omega_{m}|^{2} + |\Omega|^{2})}}$$
(2)

with  $\Omega$  being the renormalized energy gap and dS<sub>p</sub> denoting an integration over the Fermi surface. To obtain an ( $\mathbf{s} + \mathbf{d}$ )-wave symmetry state, we assume that the order parameter and energy gap can be written in the form

$$\Delta(\mathbf{k}, \omega_{\mathbf{n}}) = \Delta_{\mathbf{s}}(\omega) + \Delta_{\mathbf{d}}(\omega)\eta(\mathbf{k}) \tag{3a}$$

and

$$\Omega(\mathbf{q}, \omega) = \Omega_{s}(\omega) + \Omega_{d}(\omega)\eta(\mathbf{q}).$$
 (3b)

Substituting the pairing interaction given by eqn. (1) and the above two eqns. (3a) and (3b) into eqn. (2), we obtain a set of coupled equations for  $\Delta_s$  and  $\Delta_d$ , which can be solved. Joynt and coworkers that in the absence of the orthorhombic distortion, the  $(\mathbf{s}+\mathbf{d})$ -wave state was an unstable one and that the stable state was the  $(\mathbf{s}+\mathbf{id})$ -wave state. Beal-Monod and Maki showed at both the microscopic and macroscopic level that the  $(\mathbf{s}+\mathbf{d})$ -wave state is possible in the presence of an orthorhombic distortion. The question of which mixed wave symmetry state best describes the HTSC is now the object of much current interests. Recently, Modre et al., suggested that an investigation of the low temperature behavior of the London penetration depth  $\lambda_L$  might be a possible way to differentiate between an orthorhombic distorted HTSC having an  $(\mathbf{s}+\mathbf{id})$ -wave symmetry OP and one having an  $(\mathbf{s}+\mathbf{d})$ -wave symmetry OP.

The effects of the spin flip scattering off the magnetic moments formed on the  $Ni^{2+}$  ions can be easily incorporated into the Eliashberg Equations by writing out the one-loop corrections to the off diagonal energy

$$W(\mathbf{q},\omega) = Z(\omega)\Omega(\mathbf{q},\omega) = \Delta(\mathbf{q},\omega) + n_i \int \frac{dS}{8\pi^3 V_f} \{|U_n(\mathbf{q}-\mathbf{k})|^2 - |U_s(\mathbf{q}-\mathbf{k})|^2\} \frac{\Omega(\mathbf{q},\omega)}{|\omega_n|}.$$
 (5)

where  $U_{n(s)}$  are the normal (spin flip) scattering potential and  $n_i$  is the concentration of the magnetic impurities. The corrections to the diagonal energy yields

$$Z(\omega) = 1 + \alpha(D)V_{iso} + n_{2i}\tau_{n} \left\{ \frac{1}{2\tau_{n}} + \frac{1}{2\tau_{n}} \right\} \frac{1}{|\omega|}$$
 (6)

where the two scattering life times are defined as

$$\frac{1}{2\tau_{n(s)}} = \iint \frac{dS\mathbf{p}}{8\pi^{3}V_{f}} \frac{dS\mathbf{k}}{8\pi^{3}V_{f}} |U_{n(s)}(\mathbf{p}-\mathbf{k})|^{2}$$
 (7)

Following the steps in ref. 10, we arrive at the following expression for the rate of depression of  $T_c$  of an  $(\mathbf{s} + \mathbf{d})$ -wave HTSC due to substitution of magnetic ions into the Cu(2) sites

$$\frac{dT_c}{dx} = \frac{\pi}{4} C^{-1} \{ (\frac{g_{si} \chi J}{1 + \chi J}) a_d - \alpha(D) B \}$$
 (8)

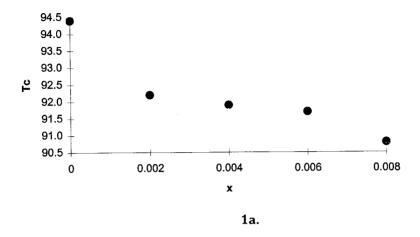
where the constants C and B depend on the various parameters which characterize the SF-mediated HTSC and which are given in refs. 10 and 12.  $a_d$  is the pair breaking parameter which appears in the Abrikosov-Gorkov theory. The exact forms of C and B are not important for the present analysis other than to say that in the limit that (D)  $\rightarrow$ 0, eqn. (8) reduces to the standard expression for the depression of  $T_c$  due to pair breaking.

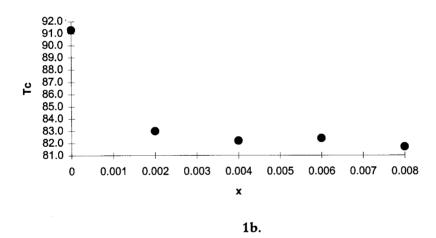
# IV. DISCUSSION.

In their study, Sumana Prahbu and Varadaraju<sup>13</sup> state "it appears at the outset that superconductivity is independent of the R ion" yet go on to say that the suppression rate due to a given impurity "ion depend on the ionic size of the rare earth (R), higher for larger R ions." They then go on and mention several possible causes of the rare earth size dependences. However, they did not come to any definte conclusions about the causes. Looking at eqn. (8), we note that the slope predicted by eqn. (8) is lowered by increasing the value of the orthorhombicity parameter (D). If our assumption that the substitution of larger rare earth ions into the layer inbetween the double CuO<sub>2</sub> retards the collapse of the CuO chains towards each other is correct, then our results from ref. 10 explains the rare earth size effect in the T<sub>c</sub>'s of the "RE-123" HTSC's and eqn. (10) of this work explains the rate earth size effect in the suppression rates dT<sub>c</sub>/dx due to magnetic ion substitution in the Cu(2) sites of the "RE-123" HTSC's.

Table 1 Lattice Parameters.

YBa <sub>2</sub> Cu <sub>3-x</sub> Ni <sub>x</sub> O <sub>7-δ</sub>	a(A)	b(A)	(b-a)/a (10-2)
x = 0.000	3.8076	3.8772	1.828
0.002	3.8071	3.8772	1.841
0.004	3.8170	3.8751	1.522
0.006	3.8133	3.8812	1.781
0.008	3.8235	3.8929	1.807
ErBa <sub>2</sub> Cu <sub>3-x</sub> Ni <sub>x</sub> O <sub>7-δ</sub>			
x = 0.000	3.8179	3.8808	1.655
0.002	3.8125	3.8804	1.784
0.004	3.8076	3.8785	1.862
0.006	3.8102	3.8797	1.824
0.008	3.8250	3.8836	1.532





**Fig.1** Depression of  $T_c$ . 1a. Of Yba<sub>2</sub>Cu<sub>3</sub>O<sub>7- $\delta$ </sub> due to Ni<sup>2+</sup> substitution into Cu (2) sites. 1b. Of ErBa<sub>2</sub>Cu<sub>3</sub>O<sub>7- $\delta$ </sub> due to Ni<sup>2+</sup> substitution.

### IV. ACKNOWLEDGMENT

One of the authors (IMT) would like to thank the Thailand Research Fund (TRF) for the financial support given while this work was being conducted. The other two authors (KK and WT) would like to thank the Department of Physics, Faculty of Science & Technology, Rangsit Campus, Thammasat University for financial assistance's. The work was done as senior projects by KK and WT at the Department of Physics.

### REFERENCES

- 1. J.G. Bednorz and K.A. Muller, (1986) Z. Phys. B 64, 189.
- 2. J.M. Tarascon et al., (1987) Phys. Rev. B 36, 226.
- 3. J.M. Tarascon et al., (1988) Phys. Rev. B 37, 7458.
- 4. P.W. Anderson, (1959) J. Phys. Chem. Solids 11, 26.
- 5. N.H. Peng and W.Y. Liang, (1994) Physica C 233, 61.
- 6. D.A. Wollman et al., (1993) Phys. Rev. Lett. 71, 2134.
- 7. C.C. Tsuei et al., (1996) Science 271, 329.
- 8. P. Monthoux and D. Pines, (1993) Phys. Rev. B 47, 6069; (1994) ibid 49, 4261.
- 9. K.A. Kouznetsov et al., (1997) Phys. Rev. Lett. 79, 3050.
- 10. I.M. Tang, S. Leelaprute and T. Osotchan, (1998) Phys. Lett A 244, 442.
- 11. J.G. Lin et al., (1995) Phys. Rev. B 51, 12,900; G.V.M. Williams and J.L. Tallon, (1996) Physica C 258, 41.
- 12. I.M. Tang, S. Leelaprute and P. Winotai, in preparation.
- 13. The values of the radii of some RE<sup>3</sup>+ ions are taken from P. Sumana Prabhu and U.V. Varadaraju, (1996) *Phys. Rev. B* **53**, 14,637.
- R. Joynt, (1990) Phys. Rev. B 41, 4271; K.A. Musaelian, J. Betouras, A.V. Chubukov and R. Joynt, (1996) ibid 53, 3598.
- M.T. Beal-Monod and K. Maki, (1996) Phys. Rev. B 53, 5775; K. Maki and M.T. Beal-Monod, (1997) ibid 55, 11,730.
- 16. R. Modre, I. Schurrer and E. Schachinger, (1998) Phys. Rev. B 57, 5496.