

Pore pressure effects on strength and elasticity of ornamental stones

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ABSTRACT: This experimental study determines the effects of pore pressure on the compressive strengths and elasticity of six ornamental stones. An approach to determine the pore pressure in low porosity rocks is presented. Rectangular rock specimens ($50 \times 50 \times 100 \text{ mm}^3$) under dry and wet conditions were axially loaded under different rates from 0.001–10 MPa/s using a polyaxial load frame. The confining pressures ranged from 0 to 12 MPa. Wet granite, marl, marble, Phra Wihan sandstone, Phu Phan sandstone, and siltstone specimens have an average water content of 0.14%, 2.7%, 0.09%, 2.05%, 4.9%, and 1.5%, respectively. Compressive shear failure was observed in specimens under slow loading rate while extension failure was found in specimens under high loading rate. The strength values of the wet specimens were lower than those of the dry ones, particularly under the high confining pressure and loading rates. The strength values obtained from the dry testing were used to quantitatively calibrate the loading rate effect from the wet strengths, and hence the effect of pore pressure could be calculated. The pore pressures notably reduced the compressive strength and elastic modulus, and slightly increased Poisson's ratio of the rocks tested.

KEYWORDS: loading rate, decorating stone, water content, elastic modulus

INTRODUCTION

The compressive strength and deformability of ornamental stones are important parameters for the applications of decorating and building stones^{1–4}. Water content can remarkably reduce the rock strength after only 1% water saturation^{5,6}. The strength of a wet specimen is lower than that of a dry one^{1,3,7–10} and the tensile strength of rocks under saturated conditions is lower than that under dry conditions^{11,12}. The influence of water on deformability of rocks is reflected as a reduction of Young's modulus and an increase of Poisson's ratio^{3,7,13,14}. The best relations between uniaxial compressive strength and elastic modulus with water content are found to be exponential functions^{5,6,9,14}. The uniaxial compressive strength and elastic modulus also decrease with increasing porosity^{4,15–17}. A simplified model for crack damage stress (σ_{cd}) in terms of porosity, elastic modulus, and Poisson's ratio has been obtained¹⁸. The model shows that when porosity decreases, the elastic modulus increases, σ_{cd} increases rapidly and approaches a maximum value. The influence of water on the strength of relatively high porosity rocks is well known. Under dry conditions, however, the quantitative effects of the pore pressures on the mechanical properties of

low porosity rock have rarely been studied. This is due to the fact that the effects of pore pressure in low porosity rocks are difficult to measure accurately¹⁹. Experimental data obtained in the 1960's concluded that for low porosity rock specimens the effective confining pressure effect is more important than pore pressure effects^{20–22}.

The objective of this study is to experimentally determine the effects of pore pressure on the compressive strengths and elasticity of six Thai ornamental stones. The effects of pore pressure on the rock strength and deformability are calculated under various loading rates and confining pressures. Both dry and wet specimens were tested. Mathematical relationships are proposed to correlate the rock mechanical properties with the pore pressure.

METHODS

Sample preparation

The rock samples used in this study are Tak granite²³, Lopburi marl and marble²⁴, Phu Phan (PP) sandstone, Phra Wihan (PW) sandstone, and Phu Kradung (PK) siltstone²⁵. They are widely used as support columns, monuments, temple walls, and footpaths. Table 1 gives the mineral compositions of the rock samples²⁶. For each rock type, 40 spec-

Table 1 Brief mineral compositions of rock samples.

Rock name	Mineral compositions and crystal/grain sizes (in mm)
Tak granite	40% plagioclase (0.5–1 mm), 30% quartz (2–5 mm), 5% orthoclase (3–5 mm), 3% amphibole (1–2 mm), 2% biotite (1–2 mm)
Lopburi marl	65% calcite (1–5 mm), 35% clay minerals (0.1–0.3 mm)
Lopburi marble	100% calcite (1–2 mm)
Phu Phan sandstone	75% quartz (0.1–0.5 mm), 15% feldspar (0.2–0.5 mm), 7% mica (0.1–0.5 mm), 3% lithic fragment (0.1–1 mm)
Phra Wihan sandstone	72% quartz (0.2–0.8 mm), 20% feldspar (0.1–0.8 mm), 3% mica (0.1–0.3 mm), 3% rock fragment (0.5–2 mm), 2% other (0.5–1 mm)
Phu Kradung siltstone	70% lithic fragment (0.1–0.3 mm), 18% quartz (0.1–0.5 mm), 7% mica (0.1–0.5 mm), 3% feldspar (0.1–0.5 mm), 2% other (0.1–0.8 mm)

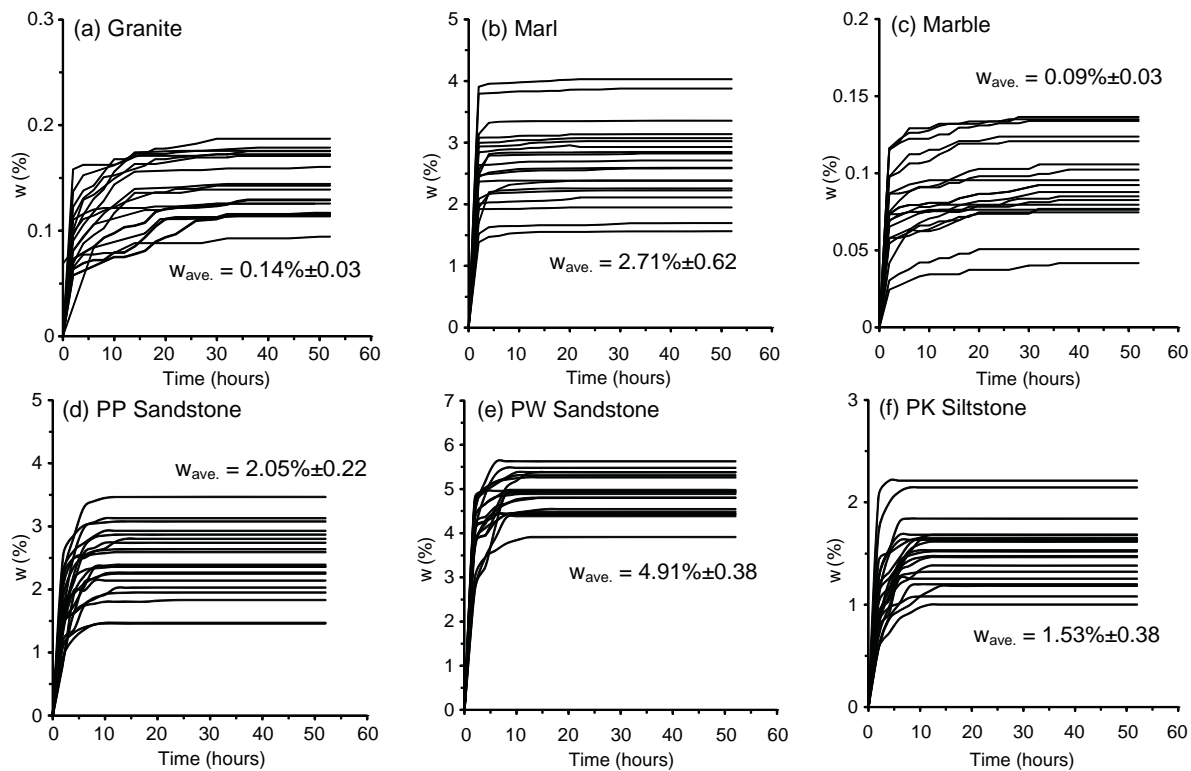


Fig. 1 Water content (w) measured as a function of time.

imens were prepared to obtain rectangular blocks with nominal dimensions of $50 \times 50 \times 100 \text{ mm}^3$ for triaxial compression tests. The specimens were cut and ground to obtain the perpendicularity and parallelism to comply with the ASTM standard practice²⁷. Testing was carried out under dry and wet conditions. Under dry condition the specimens were dried in an oven for 24 h before testing. To wet the rock specimens, they were submerged in water in a pressure vacuum chamber at a negative pressure of 0.1 MPa. The vacuum chamber was connected

to a vacuum pump (Air pump Sparmax Model TC-501V) capable of inducing -1 atm . Their weights were measured every two hours. The measurements were made outside the vacuum chamber, then the specimens were returned to the chamber. This pressure treatment was repeated until the weight remained unchanged. The average water content (w_{ave}) of granite, marl, marble, PP sandstone, PW sandstone, and siltstone was 0.14%, 2.7%, 0.09%, 2.05%, 4.9%, and 1.5%, respectively (Fig. 1).

Table 2 summarizes the physical properties of

Table 2 Physical properties of rock specimens.

Rock types	Dry density (g/cm ³)	Wet density (g/cm ³)	Water content <i>w</i> (%)	Effective porosity <i>n</i> (%)
Granite	2.64 ± 0.04	2.65 ± 0.06	0.14 ± 0.03	0.37 ± 0.06
Marl	2.49 ± 0.05	2.55 ± 0.05	2.71 ± 0.62	6.7 ± 1.4
Marble	2.74 ± 0.04	2.74 ± 0.04	0.09 ± 0.03	0.26 ± 0.07
PP Sandstone	2.42 ± 0.05	2.47 ± 0.04	2.05 ± 0.22	4.97 ± 0.51
PW Sandstone	2.25 ± 0.06	2.36 ± 0.04	4.91 ± 0.38	11.00 ± 0.97
PK Siltstone	2.53 ± 0.03	2.57 ± 0.02	1.53 ± 0.38	3.88 ± 0.98

the rock specimens.

Testing equipment and methods

The triaxial compression tests were performed on dry and wet specimens using a polyaxial load frame²⁸. The polyaxial load frame applies constant lateral and axial stresses to rectangular rock specimens. Two pairs of 152 cm long cantilever beams were used to apply the lateral loads in mutually perpendicular directions. The outer end of each beam was pulled down by a dead weight placed on a lower steel bar linking the two opposite beams underneath. The beam inner end was hinged by a pin mounted between vertical bars on each side of the frame. During testing, all beams were arranged nearly horizontally, and hence a lateral compressive load results on the specimen was placed at the centre of the frame. The maximum lateral load was designed for 100 kN. The axial load was applied with a 1000-kN hydraulic load cell connected to an electric oil pump via a pressure regulator. Constant and uniform axial and lateral stress pressures (confining pressures) were first applied to the rock specimens while the axial stress was increased at a constant rate until a failure occurred. In this study, the lateral stresses were equal, ranging 0, 3, 7, and 12 MPa, and the constant axial loading rates ranged 0.001, 0.01, 0.1, 1, and 10 MPa/s. Perforated neoprene sheets were placed at the interface between loading platens and rock surfaces to minimize the friction while allowing seepage for wet testing. The test was started by increasing the axial stress at the predefined rate using the electric pump and load cell. The axial and lateral strains were monitored by displacement gages with the accuracy of 0.001 mm. The failure stresses were recorded and the mode of failure was examined.

RESULTS

Fig. 2 shows some post-test marble specimens under confining pressures (σ_3) of 0, 3, 7, and 12 MPa with loading rates ($\partial\sigma_1/\partial t$) of 1 and 0.001 MPa/s

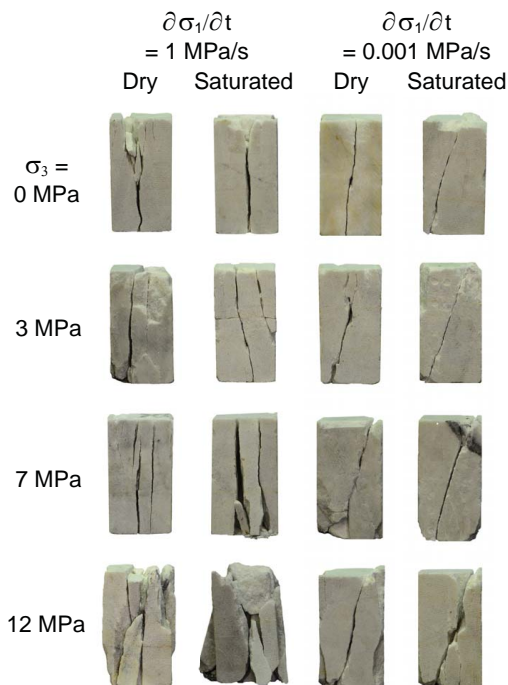


Fig. 2 Some post-test marble specimens with loading rate of 1 and 0.001 MPa/s.

for both dry and wet conditions. Compressive shear failure was observed for low loading rate specimens while extension failure was found in the high loading rate specimens. High confining pressures resulted in multiple shear fractures. Figs. 3 and 4 show the stress-strain curves obtained from different loading rates and confining pressures. The stress-strain relations are nonlinear, particularly under low loading rates. Rock specimens under high loading rate showed a higher strength than those under low loading rate (Table 3). This effect becomes larger under higher confining pressures (Fig. 5) as has been observed in other studies^{8,28,29}. The strength of the dry specimens was always greater than that of the wet one as has been found for Denizli travertine¹, homogeneous

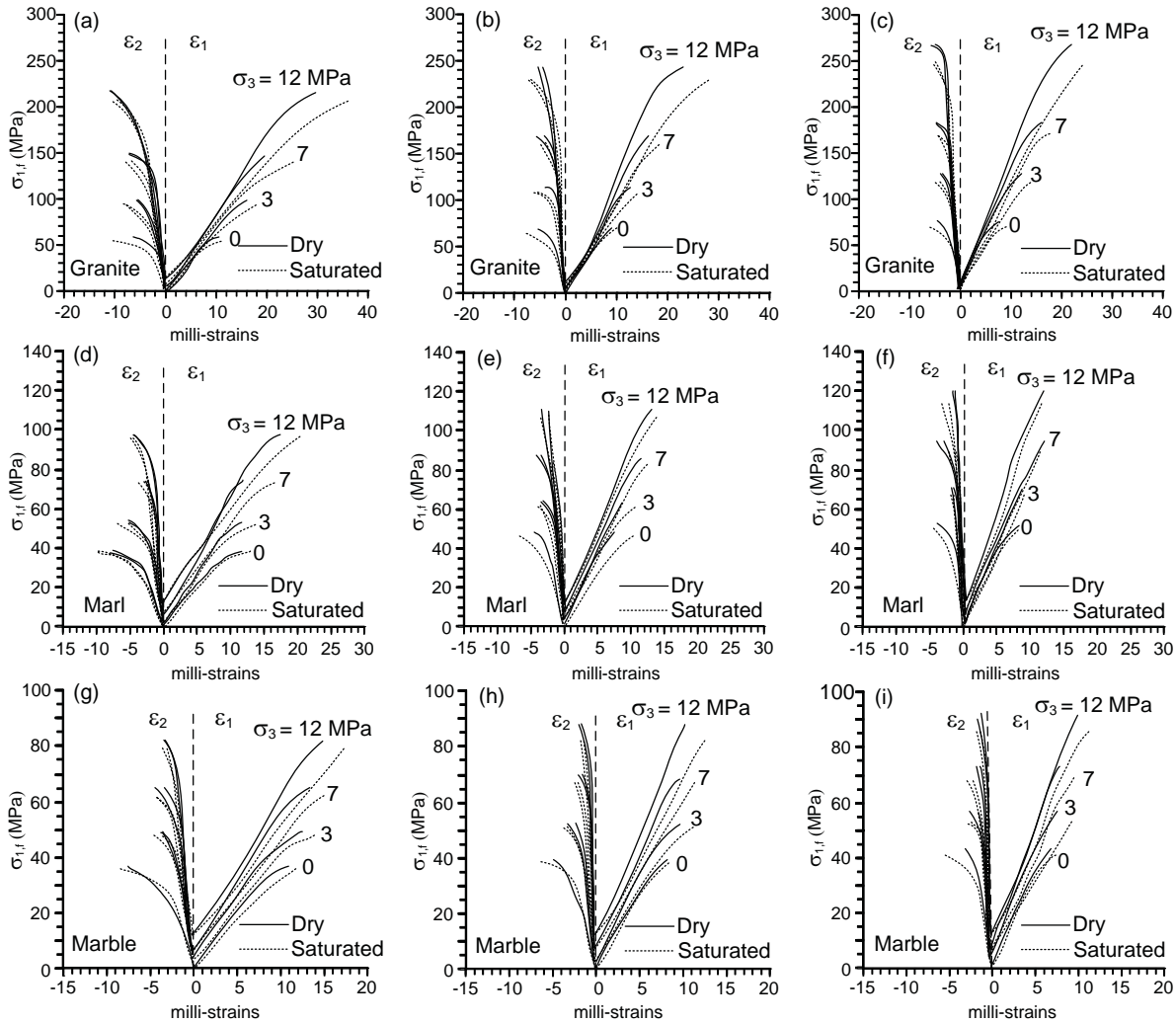


Fig. 3 Stress-strain curves obtained from (a–c) granite, (d–f) marl, and (g–i) marble specimens with loading rates of (a, d, g) 0.001 MPa/s, (b, e, h) 0.1 MPa/s, and (c, f, i) 1 MPa/s.

Indian granite⁸, sandstone^{3,7,9}, and limestone^{3,7}. The differences in strengths between the wet and dry specimens increased with confining pressures. The rock specimens with higher porosity (PW sandstone) yielded larger strength difference than those with lower porosity (granite, marl, marble, PP and PK sandstones).

Assuming that the rock specimens are linearly elastic and isotropic, the elastic modulus and Poisson’s ratio of the rocks can be determined using the following equations³⁰:

$$\begin{aligned} \varepsilon_1 &= \sigma_1/E_1 - \nu(\sigma_2/E_2 + \sigma_3/E_3) \\ \varepsilon_2 &= \sigma_2/E_2 - \nu(\sigma_1/E_1 + \sigma_3/E_3) \\ \varepsilon_3 &= \sigma_3/E_3 - \nu(\sigma_1/E_1 + \sigma_2/E_2) \end{aligned}$$

where ε_1 is the major principal strain (axial), ε_2 ,

and ε_3 are the lateral principal strains (measured separately), E_1 is the elastic modulus along the major principal directions, E_2 and E_3 are the elastic moduli along the minor principal directions, and ν is Poisson’s ratio for each specimen. The elastic parameters are determined from the tangent of stress-strain curves at 50% failure stress. In this study the lateral confining stress coefficients were equal ($\sigma_2 = \sigma_3$).

The results show that the elastic moduli increased with loading rate (Fig. 6). The elastic moduli of the dry specimens were higher than those of the wet specimens. Poisson’s ratios of dry specimens were slightly lower than those of the wet specimens (Fig. 7). These results generally agree with the results obtained on low porosity meta-sedimentary rocks¹³, on sandstone and limestone^{3,7}, and on

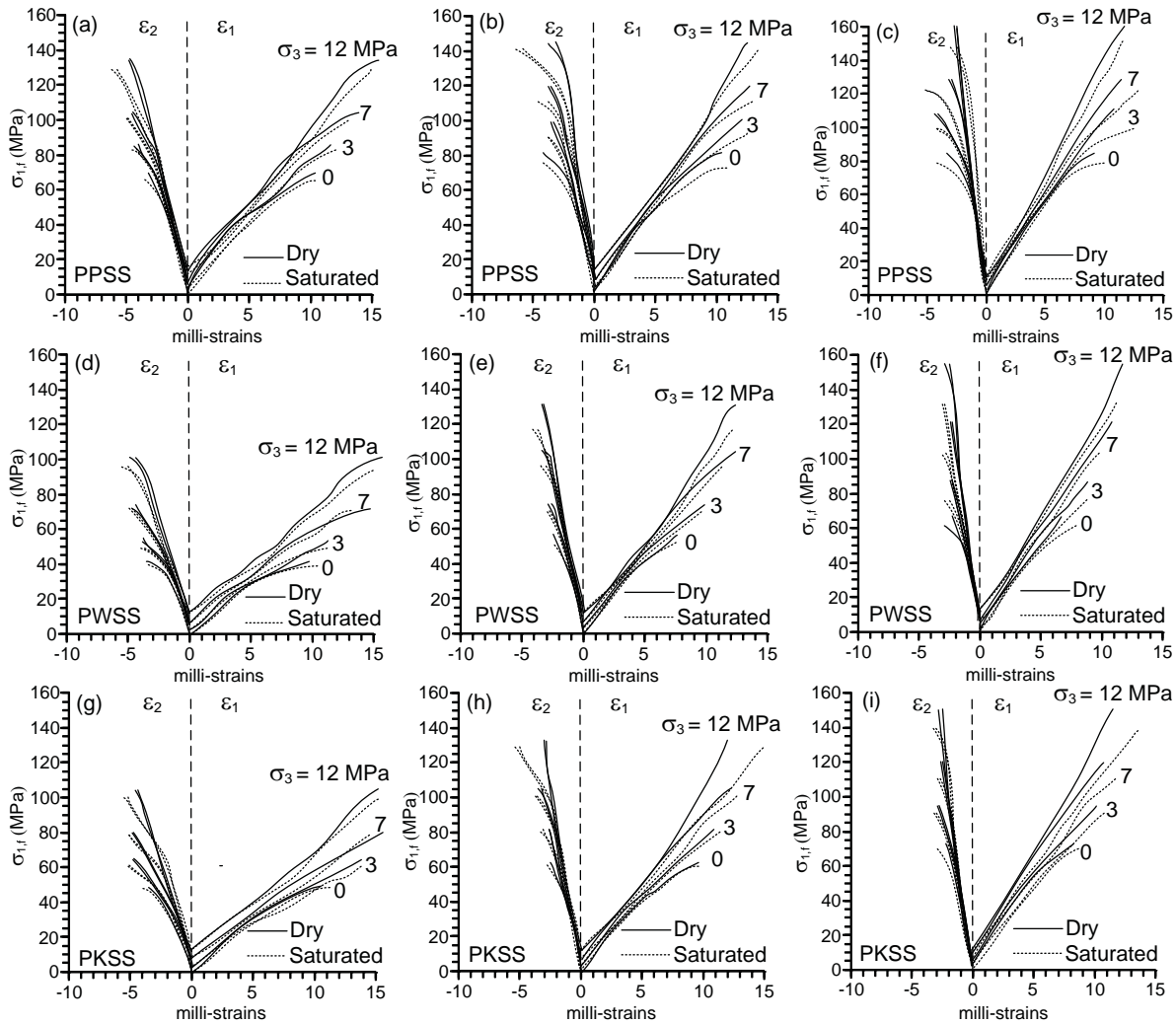


Fig. 4 Same as Fig. 3 for (a–c) PP sandstone, (d–f) PW sandstone, and (g–i) PK siltstone specimens.

gypsum¹⁴. Under a loading rate of 0.001 MPa/s the elastic modulus and Poisson’s ratio under dry and wet conditions were comparable. This suggests that the pore pressure has an insignificant effect on the rock strengths if there is sufficient time to allow water to flow out of the specimens. The elastic modulus (E) and Poisson’s ratio (ν) can be presented as a function of the loading rate as

$$E = v \left(\frac{\partial \sigma_1}{\partial t} \right)^\chi \quad (1)$$

$$\nu = \eta \ln \left(\frac{\partial \sigma_1}{\partial t} \right) + \iota \quad (2)$$

where v , χ , η , and ι are empirical constants (Figs. 6 and 7). A power function can be used to describe the increase of rock elastic modulus with the loading rate³¹. The above equations were used to calibrate

the loading rate effect on the rock strengths in the next section.

Calibrating loading rate effects

This section describes the effect of loading rate on the strengths of wet specimens, and hence reveals the effect of effective confining pressure. Here, $\sigma_{1,f,dry}$ represents the original strength of dry specimens under various loading rates and confining pressures. $\sigma_{1,f,dry}^*$ is taken here as the adjusted strength of dry specimens corresponding to $\partial \sigma_1 / \partial t = 0.1$ MPa/s. The increase of the strengths with loading rate can be represented by a logarithmic function:

$$\sigma_{1,f,dry} = \alpha \ln \left(\frac{\partial \sigma_1}{\partial t} \right) + \beta \quad (3)$$

where α and β are empirical constants (Table 4).

Table 3 Major principal stresses at failure $\sigma_{1,f}$ (MPa) under various confining pressures σ_3 and loading rates $\partial\sigma_1/\partial t$.

σ_3 (MPa)	$\partial\sigma_1/\partial t$ (MPa/s)	Granite		Marl		Marble		PP Sandstone		PW Sandstone		PK Siltstone	
		Dry	Sat.	Dry	Sat.	Dry	Sat.	Dry	Sat.	Dry	Sat.	Dry	Sat.
0	0.001	59	54	38	38	37	36	68	67	41	39	46	45
	0.01	64	59	42	41	38	37	76	74	48	48	58	57
	0.1	70	64	47	46	40	39	80	79	54	51	65	64
	1	77	70	53	51	43	41	85	82	67	60	74	72
	10	86	78	62	58	46	44	93	87	79	66	80	77
3	0.001	99	93	53	52	49	48	87	85	53	51	65	59
	0.01	104	98	57	56	51	49	93	91	65	63	75	72
	0.1	114	107	63	61	53	52	98	94	73	70	83	80
	1	128	119	71	67	56	53	108	100	86	76	95	90
	10	142	128	81	73	62	56	121	106	103	80	103	94
7	0.001	147	140	74	72	65	63	104	102	71	69	80	77
	0.01	158	150	79	77	67	65	110	107	87	86	97	92
	0.1	169	159	85	81	69	67	118	114	103	95	105	102
	1	182	169	93	88	73	69	131	124	120	103	120	112
	10	203	181	103	93	82	73	142	127	134	105	130	116
12	0.001	214	205	99	97	83	80	130	127	100	95	106	100
	0.01	225	214	104	102	85	82	138	133	120	110	123	117
	0.1	243	229	111	107	88	84	146	139	130	118	134	130
	1	267	248	120	114	93	87	157	147	154	130	152	140
	10	-	-	130	118	103	92	167	152	178	130	161	145

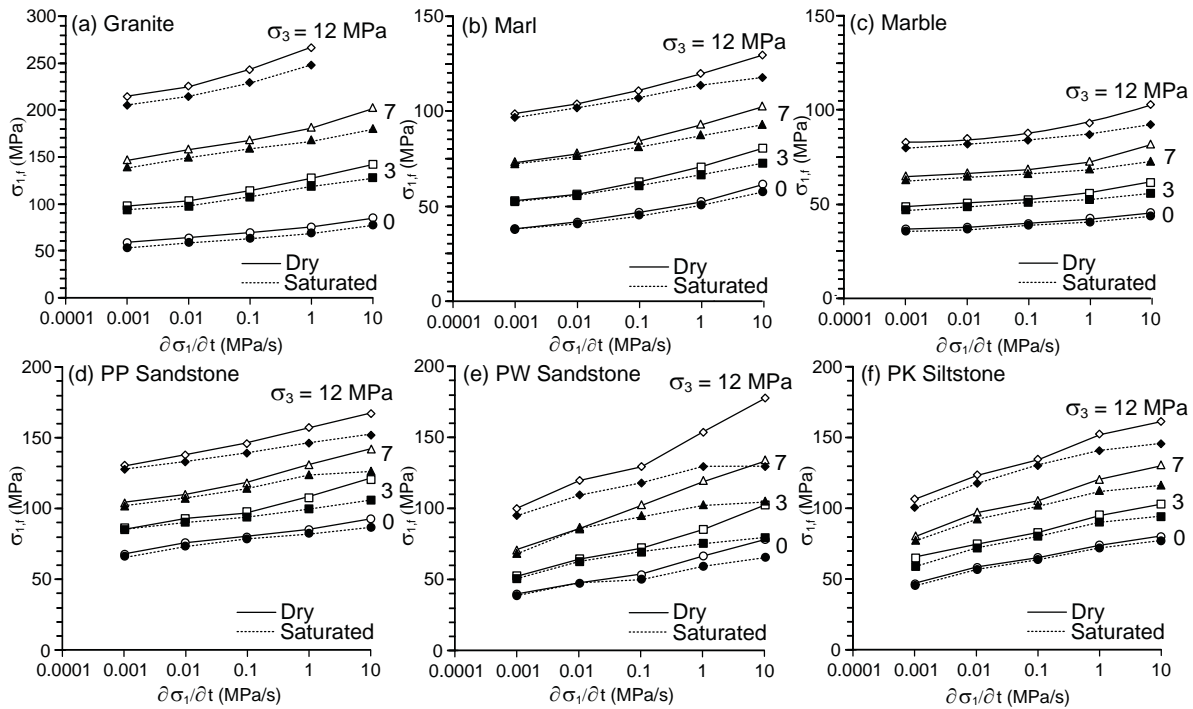


Fig. 5 Major principal stress ($\sigma_{1,f}$) as a function of loading rate ($\partial\sigma_1/\partial t$).

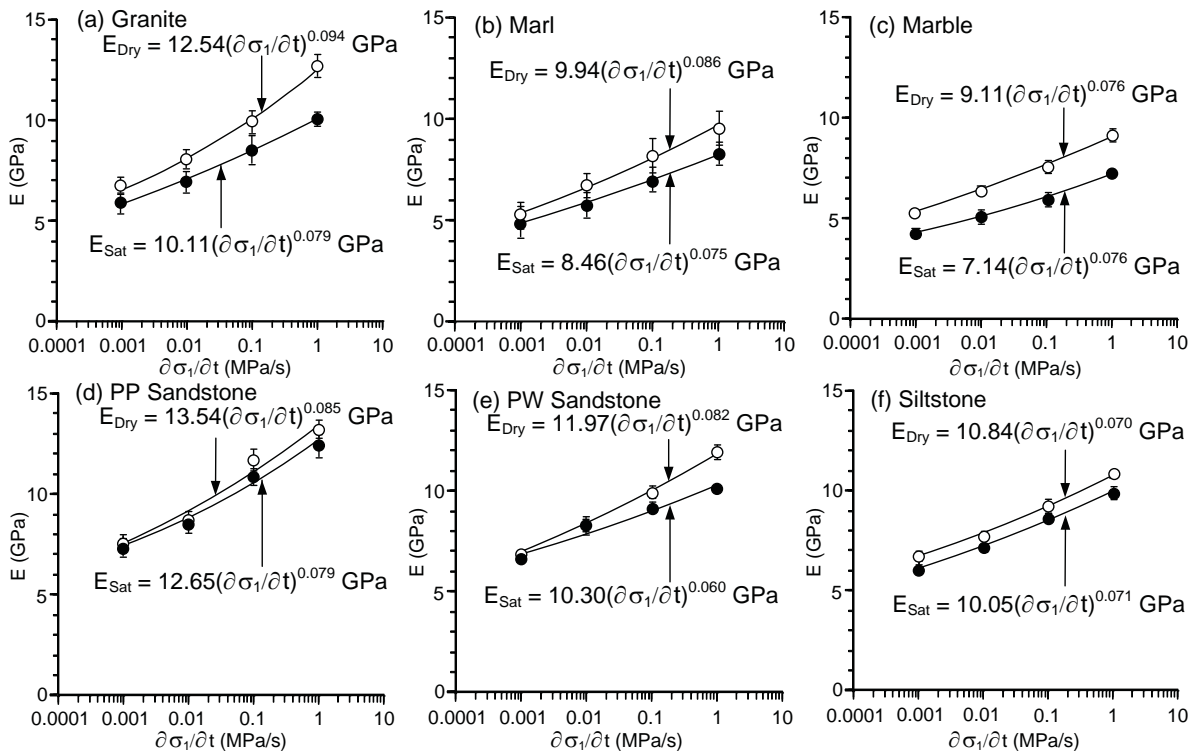


Fig. 6 Elastic modulus (E) calculated as a function of loading rate ($\partial\sigma_1/\partial t$).

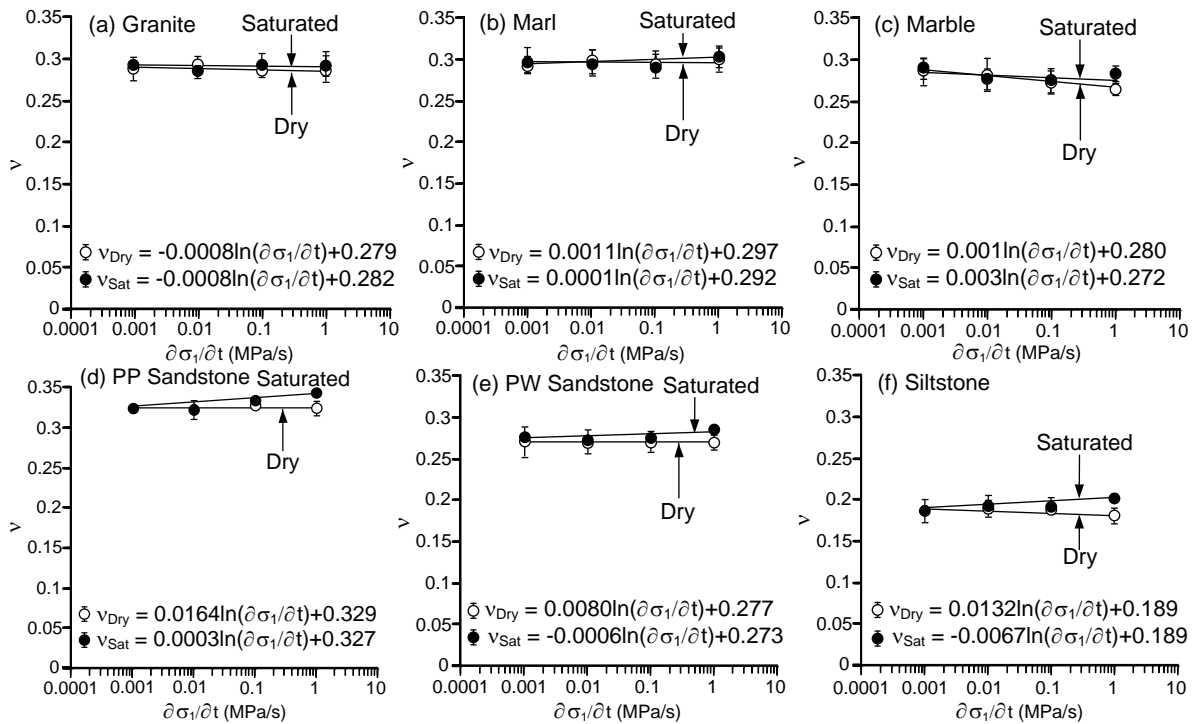


Fig. 7 Poisson's ratio (ν) calculated as a function of loading rate ($\partial\sigma_1/\partial t$).

Table 4 Empirical constants α and β for strength and loading rate relation under dry condition.

Rock types	σ_3 (MPa)	α (1/s)	β (MPa)
Granite	0	2.881	77.77
	3	4.801	128.31
	7	5.906	185.40
	12	7.643	263.56
Marl	0	2.547	54.27
	3	3.053	71.97
	7	3.192	93.95
	12	3.431	120.60
Marble	0	0.999	43.10
	3	1.351	57.30
	7	1.737	75.20
	12	2.085	95.20
PP Sandstone	0	2.536	86.18
	3	3.605	109.70
	7	4.004	130.70
	12	4.213	156.82
PW Sandstone	0	4.123	67.30
	3	5.255	88.10
	7	6.918	118.87
	12	8.247	155.41
PK Siltstone	0	3.648	73.00
	3	4.169	93.80
	7	5.368	118.82
	12	6.019	149.04

To correlate the specimen strength under identical confining pressure but with different loading rates, (3) can be rewritten as

$$\sigma_{1,f,dry} = \alpha \ln \left(\frac{\partial \sigma_1}{\partial t} \right)_i + \beta \quad (4)$$

$$\sigma_{1,f,dry}^* = \alpha \ln 0.1 + \beta \quad (5)$$

where $\sigma_{1,f,dry}$ is the strength of any dry specimen, $\sigma_{1,f,dry}^*$ is the strength of the dry specimen tested under loading rate of 0.1 MPa/s. Subtracting (4) from (5), we obtain:

$$\sigma_{1,f,dry}^* = \sigma_{1,f,dry} + \alpha \left[\ln 0.1 - \ln \left(\frac{\partial \sigma_1}{\partial t} \right)_i \right]. \quad (6)$$

Assuming that the effects of loading rate equally act on the dry and wet specimens, the adjusted strengths obtained from the dry testing are used to quantitatively correct for the loading rate effect arising from the wet testing. The adjusted strengths of the wet specimens can therefore be calculated

from:

$$\begin{aligned} \Delta \sigma_{1,f,dry}^* &= \sigma_{1,f,dry} - \sigma_{1,f,dry}^* \\ \sigma_{1,f,wet}^* &= \sigma_{1,f,wet} - \Delta \sigma_{1,f,wet}^* \end{aligned}$$

with $\Delta \sigma_{1,f,wet}^* = \Delta \sigma_{1,f,dry}^*$.

Fig. 8 shows the adjusted strengths plotted as a function of confining pressure under dry and wet conditions for the equivalent loading rate of 0.1 MPa/s. For both conditions, compressive strengths increase principal stress linearly with the confining pressure. The adjusted wet strengths are lower than those of the dry ones.

The Mohr-Coulomb criterion is applied to calculate the influence of the pore pressure under a triaxial stress state³²:

$$\sigma'_{1,f} - \sigma'_3 = \sigma_c + \sigma'_3 \left[\tan^2 \left(\frac{\pi}{4} + \frac{\phi}{2} \right) - 1 \right] \quad (7)$$

where $\sigma'_{1,f}$ is the effective strength, σ'_3 is the confining pressure, σ_c is the uniaxial compressive strength, and ϕ is the internal friction angle.

Based on the Coulomb strength criterion the cohesion (c) and internal friction angle (ϕ) of the rocks can be determined. The Coulomb criterion in terms of the principal stress coefficients at the failure ($\sigma_{1,f}$, $\sigma_{3,f}$) and the uniaxial compressive strength (σ_c) can be written as³⁰:

$$\sigma_{1,f} = \sigma_c + \sigma_{3,f} \tan^2 \alpha \quad (8)$$

$$c = \frac{\sigma_c}{2 \tan \alpha} \quad (9)$$

$$\phi = 2\alpha - \pi/2. \quad (10)$$

The cohesion and friction angle of intact rock can be obtained from regression analyses of the compressive strength data³⁰. These data include one value of uniaxial compressive strength (σ_c) and a set of major ($\sigma_{1,f}$) and minor ($\sigma_{3,f}$) principal stresses at failure obtained under the same loading rate (Table 3 and Fig. 5). The regression is performed on (8) by using σ_c , and $\sigma_{1,f}$ and $\sigma_{3,f}$ coefficients (under dry condition with the same loading rate) as input to obtain a constant parameter α (as output). The regression results show good correlation ($R^2 \geq 0.9$) between (8) and the test data (Table 5). The parameter α is then used to calculate the cohesion and friction angle by using (9) and (10). The c and ϕ values for each loading rate are summarized in Table 5 and are plotted as a function of loading rate in Fig. 9. They tend to increase with loading rate for all rock types, which supports the results shown in Fig. 5 that rocks under

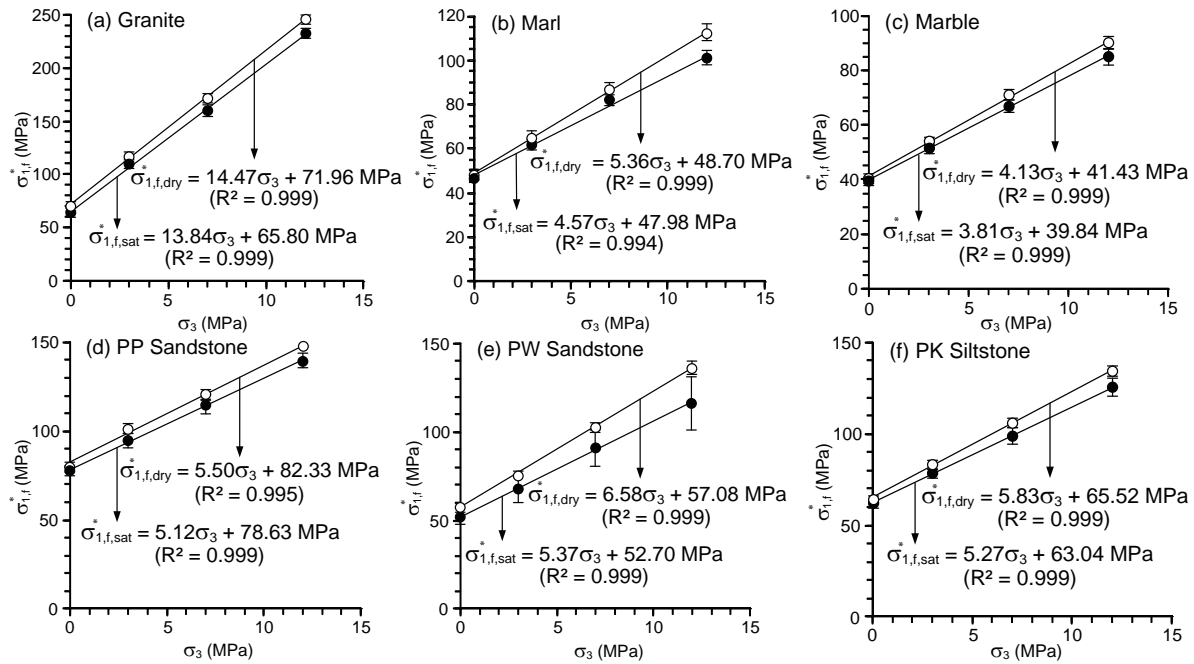


Fig. 8 Adjusted strengths ($\sigma_{1,f}^*$) as a function of confining pressure (σ_3).

Table 5 Cohesions, friction angles and coefficients of correlation under dry condition for each loading rate.

$\partial \sigma_1 / \partial t$	Parameters	Granite	Marl	Marble	PP Sandstone	PW Sandstone	PK Siltstone
0.001	c (MPa)	8.1	8.1	9.5	15.1	9.1	10.6
	ϕ (degrees)	58	41	36	42	42	41
	R^2	0.986	0.972	0.979	0.985	0.984	0.996
0.01	c (MPa)	8.7	9.3	9.8	16.4	10.1	11.8
	ϕ (degrees)	59	42	36	42	46	44
	R^2	0.985	0.973	0.982	0.981	0.977	0.993
0.1	c (MPa)	9.4	10.4	10.2	17.6	11.2	13.0
	ϕ (degrees)	60	42	36	43	47	45
	R^2	0.976	0.972	0.964	0.996	0.998	0.982
1	c (MPa)	10.0	11.6	10.5	18.9	12.3	14.2
	ϕ (degrees)	61	43	36	43	47	45
	R^2	0.973	0.963	0.988	0.995	0.992	0.987
10	c (MPa)	10.6	12.7	10.9	20.1	13.3	15.4
	ϕ (degrees)	63	43	37	45	52	49
	R^2	0.971	0.985	0.974	0.975	0.996	0.981

high loading rate show a higher strength than those under low loading rate. The highest friction angles are obtained from the granite specimens because they are composed mainly of crystalline quartz and plagioclase and have low porosity. Nevertheless, the mineral compositions are also one of the main factors governing the friction angles. This is evidenced by the fact that the low porosity marble shows lower friction angle than those of the sandstones. This is because the marble specimens are composed

mainly of calcite while the sandstone specimens are composed of stronger minerals (quartz, feldspar and lithic fragment), and hence show higher friction angle.

Since differential stress is unaffected by the pore pressure, (7) can be rewritten as

$$\sigma_{1,f,wet}^* - \sigma_3 = \sigma_{c,f,dry}^* + (\sigma_3 - P_w) \left[\tan^2 \left(\frac{\pi}{4} + \frac{\phi}{2} \right) - 1 \right] \quad (11)$$

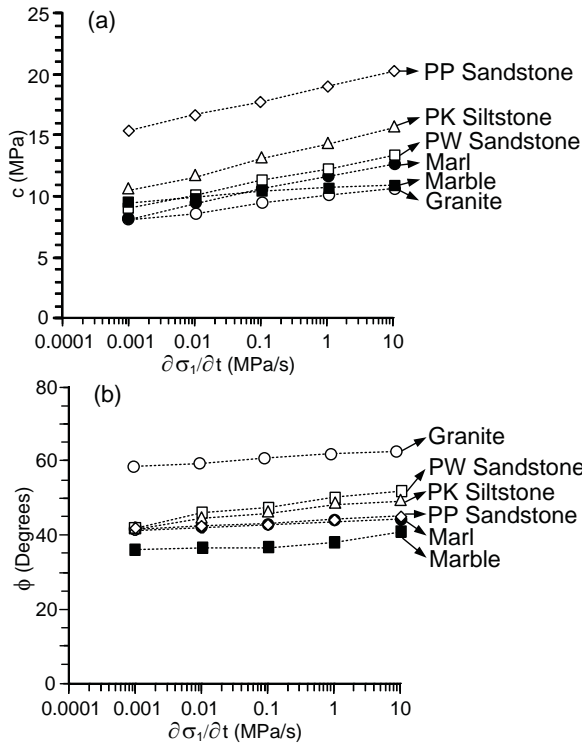


Fig. 9 (a) Cohesions and (b) friction angles as a function of loading rate for the dry condition.

where P_w is pore pressure. Solving for P_w in (11) the following relation can be obtained:

$$P_w = \sigma_3 - \frac{\sigma_{1,f,wet}^* - \sigma_3 - \sigma_{c,f,dry}^*}{\tan^2\left(\frac{\pi}{4} + \frac{\phi}{2}\right) - 1} \quad (12)$$

Fig. 10 shows the adjusted strengths as a function of pore pressure. The data are fitted to the linear equation:

$$\sigma_{1,f,wet}^* = \lambda + \kappa \sigma_3 + \xi P_w \quad (13)$$

where parameters λ , κ , and ξ are empirical constants. The adjusted strengths decrease linearly with increasing pore pressure. For all six rock types, it is apparent that the strength of the higher porosity rock (PW sandstone) is more sensitive to the pore pressure than those of the low porosity rock (granite, marl, and marble) in agreement with published results⁹.

As with the strength adjustment above, the effect of loading rate can be calibrated on the elastic parameters determined from the wet specimens. E_{dry} and ν_{dry} represent the original elastic modulus

and Poisson's ratio of dry specimens under various loading rates and confining pressures. E_{dry}^* and ν_{dry}^* represent the adjusted elastic modulus and Poisson's ratio of dry specimens tested under $\partial \sigma_1 / \partial t = 0.1$ MPa/s. The variations of the elastic modulus and Poisson's ratio with loading rate can be derived from (1) and (2). As with (6) it can be rewritten in a correlated form as

$$E_{dry}^* = E_{dry} + \nu \left[0.1^\lambda - \left(\frac{\partial \sigma_1}{\partial t} \right)_i^\lambda \right] \quad (14)$$

$$\nu_{dry}^* = \nu_{dry} + \eta \left[\ln 0.1 - \ln \left(\frac{\partial \sigma_1}{\partial t} \right)_i \right]. \quad (15)$$

The adjusted elastic modulus and Poisson's ratio of the wet specimens can be determined as

$$E_{wet}^* = E_{wet} - (E_{dry} - E_{dry}^*) \quad (16)$$

$$\nu_{wet}^* = \nu_{wet} - (\nu_{dry} - \nu_{dry}^*). \quad (17)$$

Figs. 11 and 12 show the adjusted elastic modulus and Poisson's ratio as a function of pore pressure. For all tested rocks, the adjusted elastic modulus values decrease linearly as the pore pressure increases. The adjusted Poisson's ratios slightly increase with pore pressure. This suggests that under the same stress condition the wet rocks can deform and dilate more than the dry ones.

An attempt is made to calculate the elastic moduli along the three loading directions. It is assumed here that Poisson's ratio (ν) of the rock is the same for all principal planes. They are averaged from all specimens for each rock types (Fig. 12). The adjusted elastic moduli along the major, intermediate, and minor principal directions (E_1^* , E_2^* , E_3^*) can be calculated in Ref. 30:

$$\epsilon_1^* = \sigma_1^* / E_1^* - \nu (\sigma_2^* / E_2^* + \sigma_3^* / E_3^*)$$

$$\epsilon_2^* = \sigma_2^* / E_2^* - \nu (\sigma_1^* / E_1^* + \sigma_3^* / E_3^*)$$

$$\epsilon_3^* = \sigma_3^* / E_3^* - \nu (\sigma_1^* / E_1^* + \sigma_2^* / E_2^*)$$

where ϵ_1^* , ϵ_2^* and ϵ_3^* are the major, intermediate, and minor principal strains at 50% strengths (Fig. 13). The elastic moduli along the three principal directions are similar, suggesting that the dry and wet specimens are isotropic. The elastic modulus values obtained from the wet specimens tend to be lower than those from the dry specimens.

DISCUSSION

After the effects of loading rate have been calibrated, the adjusted strengths from the wet specimens decrease with increasing pore pressure. When

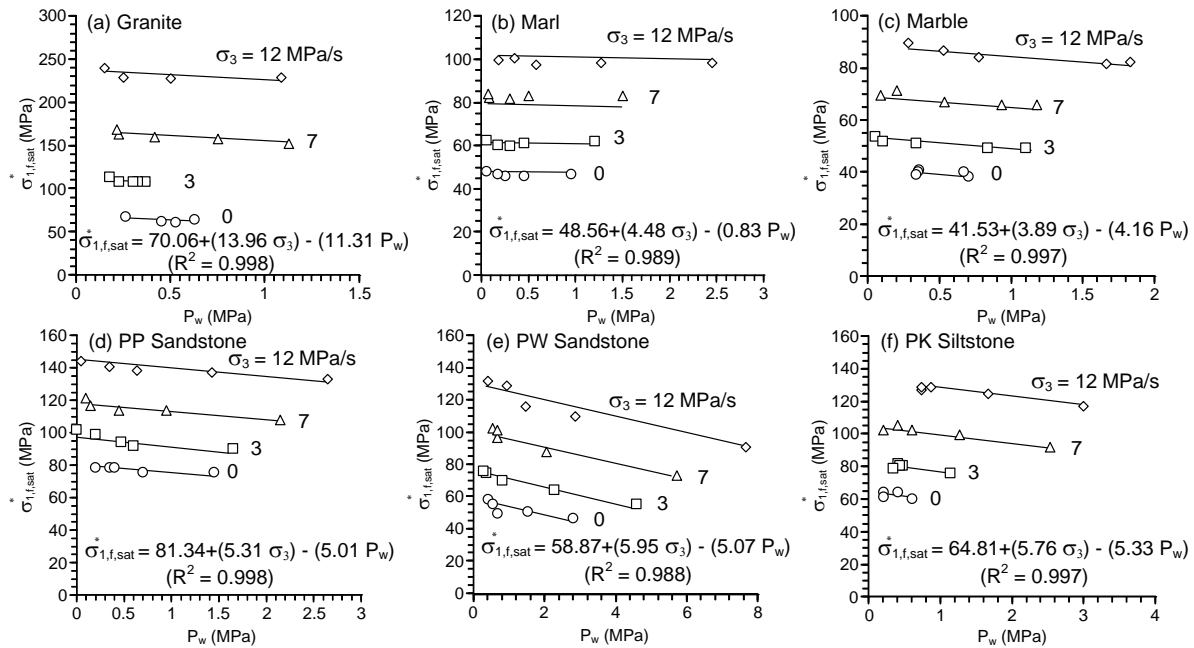


Fig. 10 Adjusted strengths ($\sigma_{1,f}^*$) as a function of pore pressure (P_w).

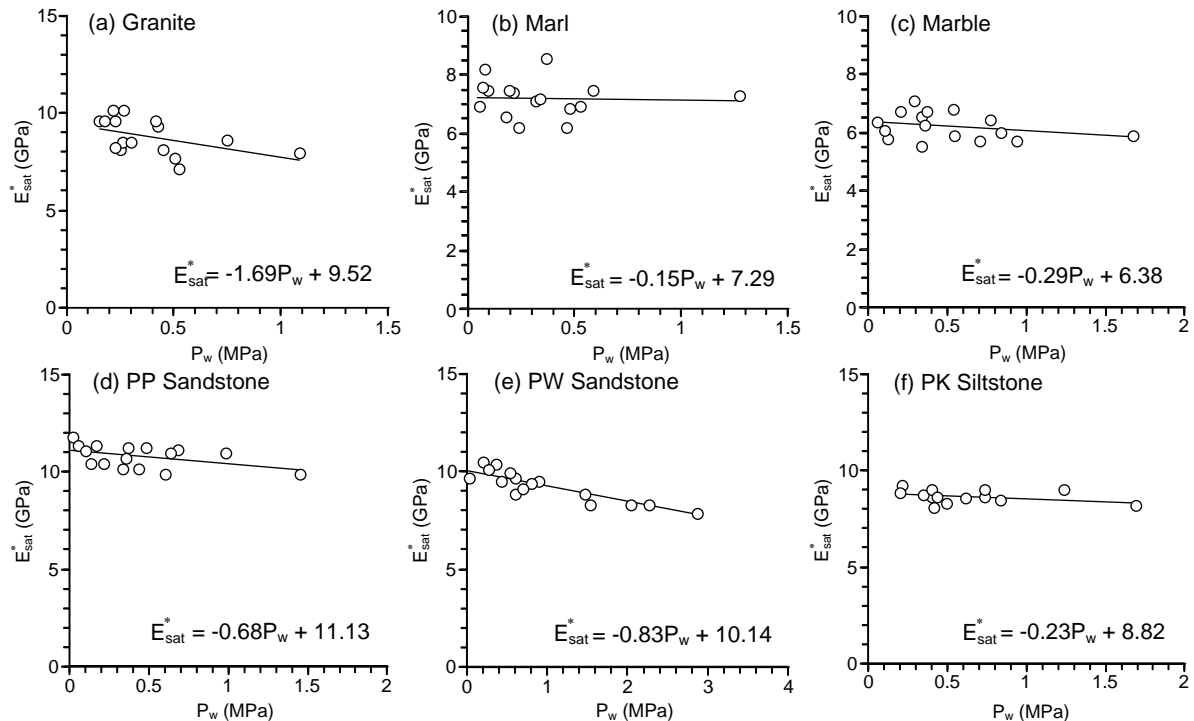


Fig. 11 Adjusted elastic modulus of wet specimen (E_{sat}^*) as a function of pore pressure (P_w).

the pore pressure increases, the elastic modulus decreased and Poisson's ratios slightly increased in agreement with experimental observations^{6,9,14}. The relations between compressive strength and

elastic modulus with pore pressure can be best represented here by linear equations in agreement with previous work²⁰.

Accuracy and reliability of the method to deter-

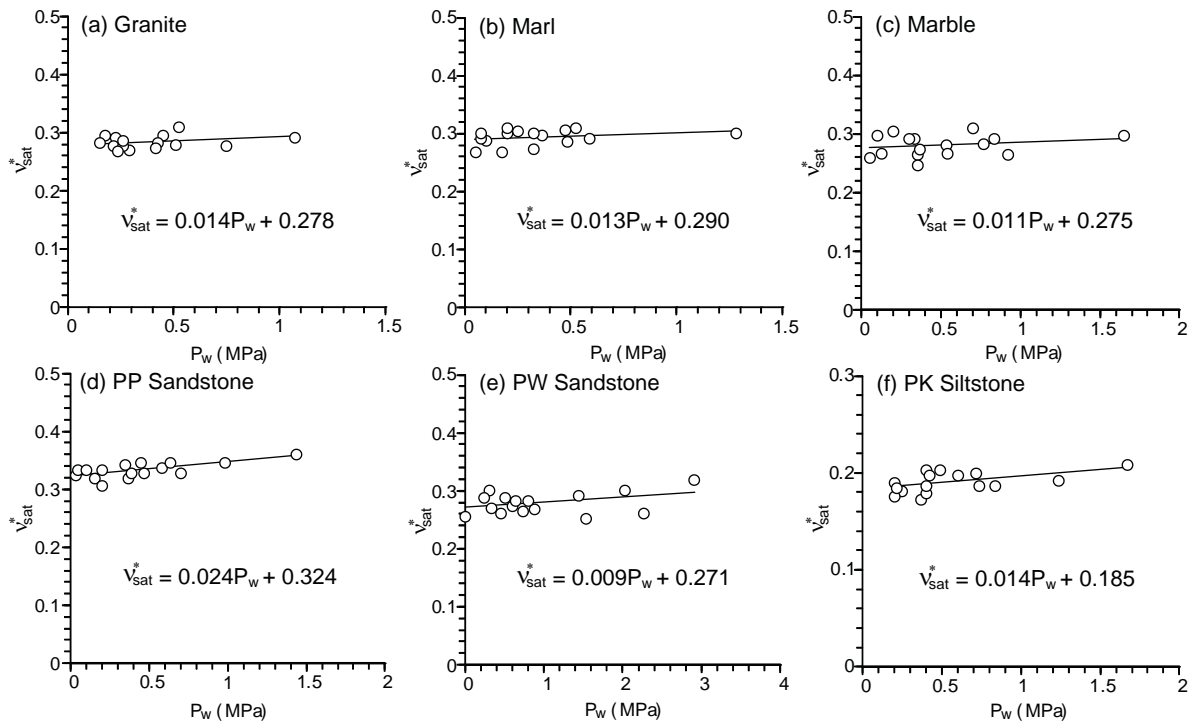


Fig. 12 Adjusted Poisson's ratio of wet specimen (ν_{sat}^*) as a function of pore pressure (P_w).

mine the effects of pore pressure proposed here depend on the range of the applied confining pressures and loading rates. A wider range of these boundary conditions may result in more accurate empirical parameters used in the equations describing the variations of the strengths, elastic moduli, and Poisson's ratios with the pore pressure. Thus a different form of the fitting equation may also be obtained. The discrepancies between the test results and the proposed equations, such as those of the elastic modulus-pore pressure relations (Fig. 11) and Poisson's ratio-pore pressure relations (Fig. 12), may be due to the intrinsic variability of the rock specimens. The large grained crystalline rocks (granite, marl, and marble) tend to show more variation than the fine grained clastic rocks (sandstones and siltstone). The water content used throughout the analysis is taken as an average value for each rock type to simplify the forms of the empirical equations used to fit the test data.

The pore spaces in the crystalline rocks are formed by the inter-crystalline boundaries and fissures while those in the clastic rocks are by the inter-granular space. The differences in the pore space characteristics cannot be detected here. Both rock groups tended to show similar effects of the pore pressure. This may be due to the fact that the tested

specimens were relatively small, with low effective porosity. For the low porosity rocks tested here the strengths are more sensitive to the confining pressure than to the pore pressure (Fig. 10). For the wet strengths the lower water content results in a lesser sensitivity the pore pressure. This suggests that the strength and deformability of low porosity rocks can be obtained from the test results under different confining pressures with more reliability than those from pore pressure determination.

Testing the wet specimens under low loading rates may represent the consolidated drained condition where the pore water has sufficient time to seep out of the rock matrix. On the other hand, the high loading rate testing may be equivalent to the consolidated undrained condition. The fast loading does not allow sufficient time for the pore water to seep out from the rock matrix. It should be noted that the maximum pore pressures determined from the proposed test method depends on the loading rate and confining pressure. A larger pore pressure magnitude may be obtained if a higher loading rate and confining pressure are applied.

This study aims at determining the effects of pore pressure on the short-term mechanical properties of ornamental and dimension stones. It is recognized that other factors not considered here do

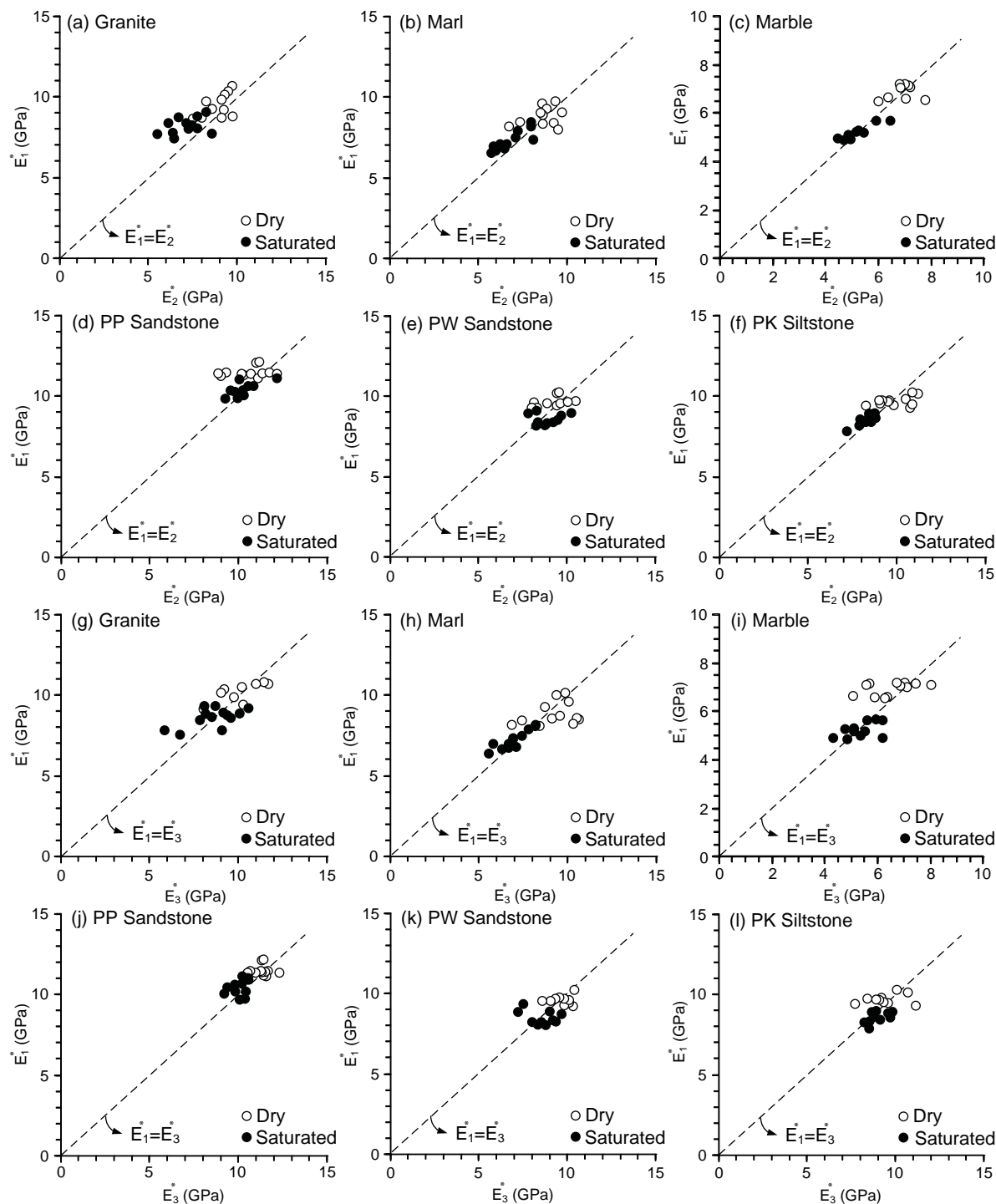


Fig. 13 Adjusted elastic modulus calculated along the major principal axis E_1^* as a function of the elastic modulus along (a–f) intermediate and (g–l) minor principal axes.

affect the rock mechanical properties under wet condition, e.g., chemical alteration, time, grain (crystal) size, propagation of micro-cracks, and fissures. The proposed method is intended for general rock

mechanics and rock engineering works, involving the well-established effective stress analysis³². The research can be readily applied by practitioner and designer for stability analysis of their decorating

and building stone. The findings can be used to assess the mechanical stability of these ornamental stones as applied under environmental conditions with various moisture contents and confinements. For example, under wet conditions if the loading rate on the rocks can be determined, the strength and deformability of the rocks can be estimated. It should be noted that in this study only one sample is tested for each loading condition. A more reliable and rigorous calibration of the rock strength and pore pressure relations may be obtained if more samples are tested under each loading and boundary condition. Nevertheless, it is believed that the main conclusions drawn above remain valid even though the number of the test specimens does not comply with the relevant ASTM standard.

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